



Proof that DE bisects AB at C:

1. $AD = DB = BE = EA$, all 4 outer line segments are the same length, by construction.
2. Since triangle ADB is isosceles, angles DAB and DBA measure the same (let's call it α_1 – Greek letters are used for angle measures.)
3. Since triangles AEB, AED, BED are also isosceles, we have 3 more pairs of congruent angles, marked α_2 , β_1 , β_2 .
4. In triangle AED, $(\alpha_1 + \alpha_2) + 2\beta_1 = 180$ degrees.
In triangle BED, $(\alpha_1 + \alpha_2) + 2\beta_2 = 180$ degrees.
Thus (subtract equations) it must be that $\beta_1 = \beta_2$.
5. In triangle ABD, $(\beta_1 + \beta_2) + 2\alpha_1 = 180$ degrees.
In triangle BED, $(\beta_1 + \beta_2) + 2\alpha_2 = 180$ degrees.
Thus it must be that $\alpha_1 = \alpha_2$.
6. Now all 4 small triangles are congruent by ASA.
7. Thus the small triangles' parts are congruent, in particular $AC = BC$, and AB is bisected.
Also all 4 angles at C are congruent and thus right.